Einstein Relation Between the Absolute Mobility and Diffusion Coefficient

Since it is a well-known fact that the diffusion of ions is simply the zig-zag walking of ions from a high-numbered region to a low-numbered region. In other words, we can say the ionic diffusion is the result of a concentration gradient in which a particular type of ions travel from a high concentration region towards a low concentration region until a homogeneity in concentration is reached. On the other hand, the conduction or the ionic migration is a result of the drift velocity component imparted to the ions by the electric force. However, it is important here to recall the fact that this velocity component does not stop the zig-zag walk of diffusion but actually gets superimposed on it. Albert Einstein understood this and formulated a relation between ionic mobility (\bar{u}_{abs}) and diffusion coefficient (D).

Now, since the conduction, as well as the diffusion, are irreversible processes, they cannot be treated by equilibrium statistical mechanics or by the equilibrium thermodynamics. However, the situation can be considered as a pseudo-equilibrium if the conduction and diffusion take place in the opposite direction but with same rates. To do so, consider an electrolytic solution of salt MX in which some of the cations are radioactive in nature. Now assume that M^+ ions are present in higher concentrations in one region and in lower concentration in some other region. In other words, the tracer ions are present with a concentration gradient. According to Fick's law of diffusion, the overall diffusion flux (J_D) must be

$$j_D = -D\frac{dc}{dx} \tag{39}$$

After applying the electric field, the tracer ions will feel the field and will start to move towards the opposite electrode. The drift velocity can be given as

$$v_d = \bar{u}_{abs} \vec{F} \tag{40}$$

The current density produced by this drift velocity is

$$J = z_{+}cFv_{d} \tag{41}$$

The conduction flux can be obtained by dividing the current density by charge carried by one mole of ions i.e.

$$j_c = \frac{z_+ cF v_d}{z_+ F} \tag{42}$$

or

$$j_c = cv_d \tag{43}$$

After using the expression of drift velocity from equation (40) in the above expression, we get

$$j_c = c \, \bar{u}_{abs} \vec{F} \tag{44}$$

The strength of the applied electric field is varied in such a way that the conduction flux and diffusion flux are equal and opposite. Mathematically, it should be like



$$j_c = -j_D \tag{45}$$

$$j_c + j_D = 0 \tag{46}$$

After using values of j_D and j_c from equations (39, 44) in the above expression, we get

$$c \,\bar{u}_{abs}\vec{F} - D\frac{dc}{dx} = 0 \tag{47}$$

or

$$\frac{dc}{dx} = \frac{c\bar{u}_{abs}\vec{F}}{D} \tag{48}$$

Since there is no net flow of ions, and therefore, this pseudo-equilibrium can be studied by Boltzmann law.

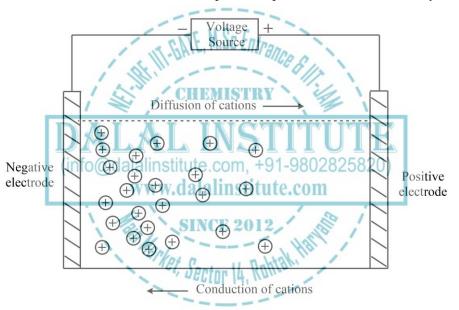


Figure 4. The pseudo-equilibrium when diffusion flux and conduction flux are equal and opposite.

Owing to the x-dependent variation, recall the ionic concentration at distance x, i.e.,

$$c = c_0 \, e^{-U/kT} \tag{49}$$

Where c_0 is the ionic concentration in the zero potential region while U is the potential energy of the ion under consideration in the externally applied electric field. Differentiating the above equation w.r.t. x, we have

$$\frac{dc}{dx} = -c_0 \, e^{-U/kT} \frac{1}{kT} \frac{dU}{dx} \tag{50}$$

Replacing $c_0 e^{-U/kT}$ by *c* i.e. using equation (49), we get



$$\frac{dc}{dx} = -\frac{c}{kT}\frac{dU}{dx} \tag{51}$$

Since the force is F = -dU/dx, the above equation takes the form

$$\frac{dc}{dx} = \frac{c}{kT}F$$
(52)

From equation (48) and equation (52), we get

$$\frac{c\bar{u}_{abs}\vec{F}}{D} = \frac{c}{kT}\vec{F}$$
(53)

$$\frac{\bar{u}_{abs}}{D} = \frac{1}{kT}$$
(54)

or

Which is the famous Einstein relation between the absolute mobility and diffusion coefficient.

Furthermore, from the phenomenological treatment of the diffusion coefficient, it is also a quite wellknown correlation that

Where B represents the undetermined phenomenological coefficient and R is the gas constant. Now, comparing equation (54) and equation (55), we have

$$\bar{u}_{abs}kT = BRT \tag{56}$$

or

$$B = \frac{\bar{u}_{abs}kT}{RT} = \frac{\bar{u}_{abs}k}{R}$$
(57)

Since N = R/k, the above equation can also be written as

$$B = \frac{\bar{u}_{abs}}{N} \tag{58}$$

It is obvious from the above equation that the phenomenological coefficient B can simply be defined as the ratio of absolute mobility to the Avogadro number. Furthermore, The Einstein relation also connects the phenomena of diffusion with force arising from viscous drag and force of electric field on the ion during its drifting movement. Therefore, the formulation also forms the basis of Stokes-Einstein (viscosity and diffusion) and Nernst–Einstein relation (equivalent conductivity and diffusion).



(54)

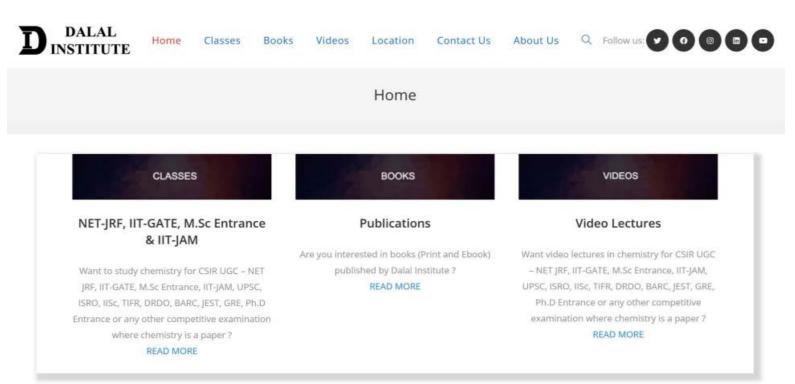
LEGAL NOTICE

This document is an excerpt from the book entitled "A Textbook of Physical Chemistry – Volume 1 by Mandeep Dalal", and is the intellectual property of the Author/Publisher. The content of this document is protected by international copyright law and is valid only for the personal preview of the user who has originally downloaded it from the publisher's website (www.dalalinstitute.com). Any act of copying (including plagiarizing its language) or sharing this document will result in severe civil and criminal prosecution to the maximum extent possible under law.



This is a low resolution version only for preview purpose. If you want to read the full book, please consider buying.

Buy the complete book with TOC navigation, high resolution images and no watermark.



Home: https://www.dalalinstitute.com/ Classes: https://www.dalalinstitute.com/classes/ Books: https://www.dalalinstitute.com/books/ Videos: https://www.dalalinstitute.com/videos/ Location: https://www.dalalinstitute.com/location/ Contact Us: https://www.dalalinstitute.com/contact-us/ About Us: https://www.dalalinstitute.com/about-us/

Postgraduate Level Classes		Undergraduate Level Classes	
(NET-JRF & IIT-GATE)		(M.Sc Entrance & IIT-JAM)	
Admission		Admission	
Regular Program Test Series	Distance Learning Result	Regular Program Test Series	Distance Learning Result

A Textbook of Physical Chemistry - Volume 1

"A Textbook of Physical Chemistry – Volume 1 by Mandeep Dalal" is now available globally; including India, America and most of the European continent. Please ask at your local bookshop or get it online here. READ MORE

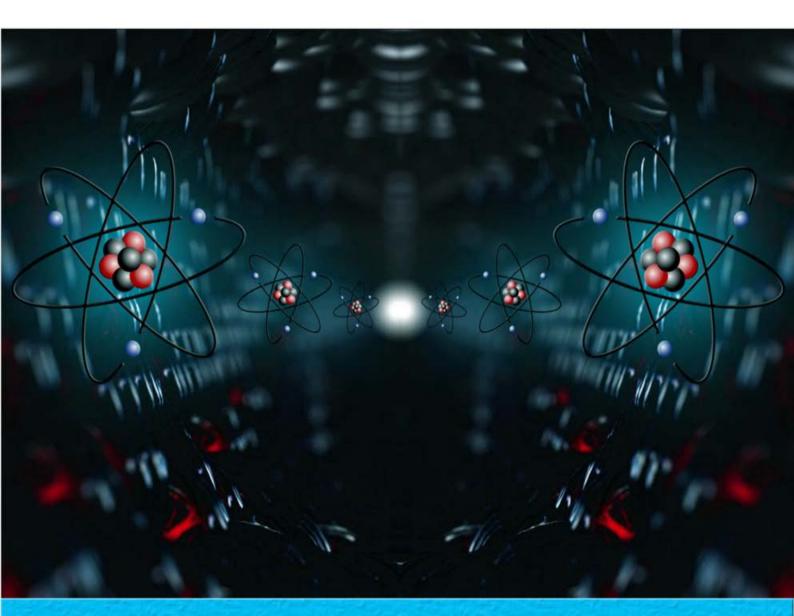
Join the revolution by becoming a part of our community and get all of the member benefits like downloading any PDF document for your personal preview.

Sign Up



A TEXTBOOK OF PHYSICAL CHEMISTRY Volume I

MANDEEP DALAL



First Edition

DALAL INSTITUTE

Table of Contents

CHAP	TER 1	11
Qua	ntum Mechanics – I	11
*	Postulates of Quantum Mechanics	11
*	Derivation of Schrodinger Wave Equation	16
*	Max-Born Interpretation of Wave Functions	21
*	The Heisenberg's Uncertainty Principle	24
*	Quantum Mechanical Operators and Their Commutation Relations	29
*	Hermitian Operators – Elementary Ideas, Quantum Mechanical Operator for Linear Mom Angular Momentum and Energy as Hermitian Operator	
*	The Average Value of the Square of Hermitian Operators	62
*	Commuting Operators and Uncertainty Principle (x & p; E & t)	63
*	Schrodinger Wave Equation for a Particle in One Dimensional Box	
*	Evaluation of Average Position, Average Momentum and Determination of Uncertainty in F and Momentum and Hence Heisenberg's Uncertainty Principle	
*	Pictorial Representation of the Wave Equation of a Particle in One Dimensional Box Influence on the Kinetic Energy of the Particle in Each Successive Quantum Level	and Its
*	Lowest Energy of the Particle	80
*	Problems	82
*	Bibliography	83
CHAP	TER 2	84
Ther	rmodynamics – I	84
*	Brief Resume of First and Second Law of Thermodynamics	84
*	Entropy Changes in Reversible and Irreversible Processes	87
*	Variation of Entropy with Temperature, Pressure and Volume	92
*	Entropy Concept as a Measure of Unavailable Energy and Criteria for the Spontaneity of R	
*	Free Energy, Enthalpy Functions and Their Significance, Criteria for Spontaneity of a Proce	ss 98
*	Partial Molar Quantities (Free Energy, Volume, Heat Concept)	104
*	Gibb's-Duhem Equation	108
*	Problems	111
*	Bibliography	112

CHAP	CHAPTER 3	
Cher	nical Dynamics – I	113
*	Effect of Temperature on Reaction Rates	113
*	Rate Law for Opposing Reactions of Ist Order and IInd Order	119
*	Rate Law for Consecutive & Parallel Reactions of Ist Order Reactions	127
*	Collision Theory of Reaction Rates and Its Limitations	135
*	Steric Factor	141
*	Activated Complex Theory	143
*	Ionic Reactions: Single and Double Sphere Models	147
*	Influence of Solvent and Ionic Strength	152
*	The Comparison of Collision and Activated Complex Theory	157
*	Problems	158
*	Bibliography	159
CHAP'	ГЕК 4	160
Elect	rochemistry – I: Ion-Ion Interactions	160
*	The Debye-Huckel Theory of Ion-Ion Interactions	160
*	Potential and Excess Charge Density as a Function of Distance from the Central Ion	168
*	Debye-Huckel Reciprocal Length	173
*	Ionic Cloud and Its Contribution to the Total Potential	176
*	Debye-Huckel Limiting Law of Activity Coefficients and Its Limitations	178
*	Ion-Size Effect on Potential	185
*	Ion-Size Parameter and the Theoretical Mean - Activity Coefficient in the Case of Ionic C Finite-Sized Ions	
*	Debye-Huckel-Onsager Treatment for Aqueous Solutions and Its Limitations	190
*	Debye-Huckel-Onsager Theory for Non-Aqueous Solutions	195
*	The Solvent Effect on the Mobility at Infinite Dilution	196
*	Equivalent Conductivity (Λ) vs Concentration $C^{1/2}$ as a Function of the Solvent	198
*	Effect of Ion Association Upon Conductivity (Debye-Huckel-Bjerrum Equation)	200
*	Problems	209
*	Bibliography	210
CHAP'	ΓER 5	211
Qua	ntum Mechanics – II	211
*	Schrodinger Wave Equation for a Particle in a Three Dimensional Box	211

*	The Concept of Degeneracy Among Energy Levels for a Particle in Three Dimensional Box	215
*	Schrodinger Wave Equation for a Linear Harmonic Oscillator & Its Solution by Polynomial	
*	Zero Point Energy of a Particle Possessing Harmonic Motion and Its Consequence	
*	Schrodinger Wave Equation for Three Dimensional Rigid Rotator	231
*	Energy of Rigid Rotator	241
*	Space Quantization	243
*	Schrodinger Wave Equation for Hydrogen Atom: Separation of Variable in Polar Sp	
	Coordinates and Its Solution	
*	Principal, Azimuthal and Magnetic Quantum Numbers and the Magnitude of Their Values	
*	Probability Distribution Function	
*	Radial Distribution Function	278
*	Shape of Atomic Orbitals $(s, p \& d)$	281
*	Problems	287
*	Bibliography	288
CHAP	ГЕR 6	289
Ther	modynamics – II	289
*	Clausius-Clapeyron Equation	289
*	Law of Mass Action and Its Thermodynamic Derivation	293
*	Third Law of Thermodynamics (Nernst Heat Theorem, Determination of Absolute E	ntropy,
	Unattainability of Absolute Zero) And Its Limitation	296
*	Phase Diagram for Two Completely Miscible Components Systems	304
*	Eutectic Systems (Calculation of Eutectic Point)	311
*	Systems Forming Solid Compounds A _x B _y with Congruent and Incongruent Melting Points	321
*	Phase Diagram and Thermodynamic Treatment of Solid Solutions	332
*	Problems	342
*	Bibliography	343
CHAP	TER 7	344
Cher	nical Dynamics – II	344
*	Chain Reactions: Hydrogen-Bromine Reaction, Pyrolysis of Acetaldehyde, Decomposit	
*	Photochemical Reactions (Hydrogen-Bromine & Hydrogen-Chlorine Reactions)	
*	General Treatment of Chain Reactions (Ortho-Para Hydrogen Conversion and Hydrogen-B	
•	Reactions)	

*	Apparent Activation Energy of Chain Reactions	362
*	Chain Length	364
*	Rice-Herzfeld Mechanism of Organic Molecules Decomposition (Acetaldehyde)	366
*	Branching Chain Reactions and Explosions (H2-O2 Reaction)	368
*	Kinetics of (One Intermediate) Enzymatic Reaction: Michaelis-Menten Treatment	371
*	Evaluation of Michaelis's Constant for Enzyme-Substrate Binding by Lineweaver-Burk H Eadie-Hofstee Methods	
*	Competitive and Non-Competitive Inhibition	378
*	Problems	388
*	Bibliography	389
СНАР	TER 8	390
Elect	trochemistry – II: Ion Transport in Solutions	390
*	Ionic Movement Under the Influence of an Electric Field	390
*	Mobility of Ions	393
*	Ionic Drift Velocity and Its Relation with Current Density	394
*	Einstein Relation Between the Absolute Mobility and Diffusion Coefficient	398
*	The Stokes-Einstein Relation	401
*	The Nernst-Einstein Equation	403
*	Walden's Rule	404
*	The Rate-Process Approach to Ionic Migration	406
*	The Rate-Process Equation for Equivalent Conductivity	410
*	Total Driving Force for Ionic Transport: Nernst-Planck Flux Equation	412
*	Ionic Drift and Diffusion Potential	416
*	The Onsager Phenomenological Equations	418
*	The Basic Equation for the Diffusion	419
*	Planck-Henderson Equation for the Diffusion Potential	422
*	Problems	425
*	Bibliography	426
INDEX	ζ	427



Mandeep Dalal (M.Sc, Ph.D, CSIR UGC - NET JRF, IIT - GATE) Founder & Director, Dalal Institute Contact No: +91-9802825820 Homepage: www.mandeepdalal.com E-Mail: dr.mandeep.dalal@gmail.com Mandeep Dalal is an Indian research scholar who is primarily working in the field of Science and Philosophy. He received his Ph.D in Chemistry from Maharshi Dayanand University, Rohtak, in 2018. He is also the Founder and Director of "Dalal Institute", an India-based educational organization which is trying to revolutionize the mode of higher education in Chemistry across the globe. He has published more than 40 research papers in various international scientific journals, including mostly from Elsevier (USA), IOP (UK) and Springer (Netherlands).







Main Market, Sector-14, Rohtak, Haryana-124001 (+91-9802825820, info@dalalinstitute.com) www.dalalinstitute.com